



## Early Journal Content on JSTOR, Free to Anyone in the World

This article is one of nearly 500,000 scholarly works digitized and made freely available to everyone in the world by JSTOR.

Known as the Early Journal Content, this set of works include research articles, news, letters, and other writings published in more than 200 of the oldest leading academic journals. The works date from the mid-seventeenth to the early twentieth centuries.

We encourage people to read and share the Early Journal Content openly and to tell others that this resource exists. People may post this content online or redistribute in any way for non-commercial purposes.

Read more about Early Journal Content at <http://about.jstor.org/participate-jstor/individuals/early-journal-content>.

JSTOR is a digital library of academic journals, books, and primary source objects. JSTOR helps people discover, use, and build upon a wide range of content through a powerful research and teaching platform, and preserves this content for future generations. JSTOR is part of ITHAKA, a not-for-profit organization that also includes Ithaka S+R and Portico. For more information about JSTOR, please contact [support@jstor.org](mailto:support@jstor.org).

4. Proposed by H. W. Holycross, Superintendent of Schools, Pottersburg, Union County, Ohio.

What value of  $x$  will render  $4x^4 + 12x^3 - 3x^2 - 2x + 1$  a square?

Solution by P. S. BERG, Apple Creek, Ohio.

Extracting the square root of the expression we get  $2x^2 + 3x - 3$  as the partial root and a remainder of  $16x - 8$ , or the expression  $= (2x^2 + 3x - 3)^2 + 16x - 8$ . Now when  $16x - 8 = 0$ , the expression is a square.  $\therefore x = \frac{1}{2}$  is the required value.

Also solved by J. H. Drummond, A. L. Foote, H. C. Whitaker, G. B. M. Zerr, and O. S. Kibler.

## PROBLEMS.

5. Proposed by ISAAC L. BEVERAGE, Monterey, Virginia.

Find three numbers the sum of the squares of any two of which diminished by their product shall be a square number.

6. Proposed by Professor G. B. M. ZERR, A. M., Principal of High School, Staunton, Virginia.

Find three whole numbers the sum of any two of which is a cube.

8. Proposed by Hon. JOSIAH H. DRUMMOND, Portland, Maine.

Every odd square is of the form  $4a + 1$ ; find the value of  $a$  for the  $n$ th consecutive odd square.

Solutions to these problems should be received on or before May 1st.

## AVERAGE AND PROBABILITY.

Conducted by B. F. FINKEL, Kidder, Missouri. All contributions to this department should be sent to him.

### SOLUTION TO A PROBLEM IN AVERAGE.

By B. F. FINKEL, A. M., Professor of Mathematics in Kidder Institute, Kidder, Missouri.

Two circles whose radii are  $R$  and  $r$  respectively, are tangent internally. Find the average area of all circles that can be drawn tangent to the two circles.

Let  $AO = R$  be the radius of the larger circle;  $AC = r$ , the radius of the smaller circle; and  $A$  the point of internal tangency of the two circles.

Let  $ID$  be any circle inscribed within the crescent,  $F$  the center of this circle,  $IF = z$ , its radius, and  $(x, y)$  the rectangular co-ordinates of the point  $F$  referred to  $A$  as the origin of co-ordinates. Draw  $FC$  and  $OD$ . Then  $OF = (R - z)$ ,  $CF = (r + z)$ ,  $CE = (x - r)$ , and  $OE = (x - R)$ . From the figure, we have  $FC^2 - CE^2 = OF^2 - OE^2$ , or  $(r + z)^2 - (x - r)^2 = (R - z)^2 - (x - R)^2$ , whence  $z = \left(\frac{R - r}{R + r}\right)x$ . We

also have  $OF^2 = OE^2 + EF^2$ , or  $(R - z)^2 = (x - R)^2 + y^2$ . Substituting the value of  $z$  and solving with respect to  $y^2$ , we have  $y^2 = \frac{4Rr}{(R + r)^2} [(R + r)x - x^2]$ ,

